of observation, the values of I,  $I_l$  and J found for non-equatorial diffuse spots must be multiplied by  $\sec^2 \chi$ ,  $\sec \chi$  and 1 respectively.

Table 1 summarizes the values found for the partial inclination factors by which the observed quantities I',  $I'_l$  and J' are to be multiplied. The total inclination factor is obtained by multiplying the three factors along the appropriate horizontal line.

The total factor for J is similar to the 'film-absorption factor' found by Cox & Shaw (1930) in their study of integrated reflexion. It is plotted in Fig. 4 (curve (b)) as a function of  $\zeta = \sin \chi$ , using Cox & Shaw's experimental values for C and  $(\mu t)$ . In the same figure,

the corresponding inclination factor for I has also been plotted (curve (a)).

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# The Crystal and Molecular Structure of B<sub>4</sub>Cl<sub>4</sub>

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The molecule  $B_4Cl_4$  consists of a nearly regular tetrahedron of boron atoms surrounded by a larger, nearly regular tetrahedron of chlorine atoms with B-Cl single bonds (1.70 Å) directed away from the center of the tetrahedra. The molecular symmetry is  $D_{2d}-\bar{4}2m$ , but differs only slightly from  $T_d-\bar{4}3m$ , and the average B-B distance is 1.70 Å. Molecular centers are at 0, 0,  $\frac{1}{2}$  and  $\frac{1}{2}$ ,  $\frac{1}{2}$ , 0 in the space group  $D_{4b}^{16}-P4_2/nmc$ , with a = b = 8.09 Å and c = 5.45 Å.

The unusual compound,  $B_4Cl_4$ , has recently been discovered by Urry, Wartik & Schlesinger (1952), who have kindly supplied us with a sample for molecular structure determination by the X-ray diffraction method. This study is part of a general program of structure determinations of electron deficient compounds of boron.

The sample was distilled carefully into thin-walled pyrex capillaries in a vacuum line previously flushed with BF<sub>3</sub> in order to remove reactive compounds adsorbed on the glass surfaces. The samples in these capillaries were stored about two weeks at about  $35^{\circ}$  C. with a small temperature gradient in the capillary in order to grow a single crystal about 0.3 by 0.5 by 1.2 mm. The symmetry of the tetragonal reciprocal lattice is  $D_{4h}$ -4/mmm. The unit-cell dimensions of

$$a = b = 8.09 \pm 0.02$$
 and  $c = 5.45 \pm 0.01$  Å

lead to a unit cell volume of 356 Å<sup>3</sup>. Assuming the usual values for van der Waals radii this unit cell must contain two molecules of  $B_4Cl_4$ , and the crystal therefore has the reasonable calculated density of 1.724 g.cm.<sup>-3</sup>. Because of the reactivity of the compound no independently measured value is known.

Buerger precession photographs of the  $\{0kl\}$ ,  $\{hhl\}$ ,  $\{h,2h,l\}$  and  $\{h,3h,l\}$  zones, and Weissenberg photographs of the  $\{hk0\}$  zone were taken with Mo  $K\alpha$ 

radiation. Intensities were estimated visually with the aid of standard scales prepared by timed exposures of a reflection from the crystal, and timed exposures of the various zones or multiple-film techniques were employed as additional aids. The revised Lorentz factor (Waser, 1951) was used in the reduction of the intensities of the precession photographs. Systematic extinctions of *hhl* when *l* is odd and of *hk0* when h+k is odd lead uniquely to the space group  $D_{4h}^{15}-P4_2/nmc$ . The presence of only two molecules in this space group requires the molecular symmetry to be  $D_{2d}-\overline{42m}$ .

Both packing considerations and the presence of fairly strong reflections which would be approximately extinguished by choice of positions 8(e) or 8(f) lead to the positions 8(g) (Internationale Tabellen, 1935, p. 222) for the chlorine atoms. The x and z parameters in these positions,

$$\begin{array}{c} 0, x, z; \ x, 0, \overline{z}; \ \frac{1}{2}, \frac{1}{2} + x, \frac{1}{2} - z; \ \frac{1}{2} + x, \frac{1}{2}, \frac{1}{2} + z; \\ 0, x, \overline{z}; \ \overline{x}, 0, \overline{z}; \ \frac{1}{2}, \frac{1}{2} - x, \frac{1}{2} - z; \ \frac{1}{2} - x, \frac{1}{2}, \frac{1}{2} + z, \end{array}$$

were estimated by trial-and-error methods with the aid of charts described by Bragg & Lipson (1936). The electron-density projections along [001] and [100] were then synthesized with the use of signs evaluated from the chlorine contributions only. Although no assumption had been made of the boron positions, these atoms appeared on the electron-density maps in



Fig. 1. Electron-density projection along the c axis. Contours are at 2 (broken), 6, 10, 14...  $e.\dot{A}^{-2}$  except around the resolved boron atoms, for which contours are at 2 (broken), 4, 6, 8  $e.\dot{A}^{-2}$ .





Fig. 3. Electron-density projection along the a axis. Contours are at levels as described for Fig. 1.

positions 8(g), and subsequent refinement was then carried out until no further sign changes occurred. These final Fourier projections are shown in Fig. 1 and 3, their interpretation is given in Figs. 2 and 4, and a plan of the molecule is shown in Fig. 5. Similar Fourier projections, carried out with the use of calculated structure factors as coefficients, gave backshift corrections for termination of the series, but resulted in no further sign changes. In addition, the parameters and their probable errors were determined



Fig. 2. Projection of the structure of  $B_4Cl_4$  on (001). The complete unit cell is shown.



Fig. 4. Projection of the structure of  $B_4Cl_4$  on (100). The complete unit cell is shown.

by least squares with the use of the method and weighting factors described by Hughes (1941). The

Table	1.	The	atomic	parameters	of	B <sub>4</sub> Cl <sub>4</sub>

	$\{hk0\}$	$\{0kl\}$	least	Weighted	Probable
	Fourier	Fourier	squares	average	errors
$x_{\mathrm{Cl}}$	0.2750	0.2750	0.2761	0.2756	0.0010
$z_{\rm Cl}$		0.2041	0.2058	0.2020	0.0009
$x_{\rm B}$	0.107	0.104	0.1036	0.1043	0.0037
$z_{\rm B}$	<u> </u>	0.385	0.3896	0.3873	0.0041

hkl	$F_o$	$F_{c}$	hkl	$F_{o}$	$F_{c}$		hkl	$F_o$	$F_{c}$
200	9.6	-8.9	024	$2 \cdot 4$	$2 \cdot 2$		0,10,1	$2 \cdot 2$	3.0
400	28.2	30.1	025	$< 2 \cdot 1$	1.1		0,10,2	$2 \cdot 0$	-2.5
600	$2 \cdot 4$	-4.9	026	$< 2 \cdot 1$	-0.1		121	11.8	-10.8
800	7.4	9.0	027	$2 \cdot 2$	-1.9		122	5.6	-5.6
10,0,0	$3 \cdot 4$	-4.6	031	$5 \cdot 1$	6.1		123	11.1	-12.5
110	4.4	-2.6	032	< 1.7	-0.3		124	6.9	-7.2
130	9.0	7.6	033	12.0	12.5		125	4.6	-4.0
150	11.6	11.6	034	5.0	-5.0		126	$4 \cdot 2$	-3.9
170	7.6	6.9	035	9.4	9.5	1	241	22.5	-21.5
190	< 4.8	3.5	036	$3 \cdot 2$	-3.3		242	< 1.6	1.2
220	41.0	-38.7	041	$5 \cdot 2$	-6.7		243	11.8	-12.8
<b>240</b>	3.6	3.9	042	19.0	19.7		244	< 1.8	-0.5
260	15.4	-15.6	043	$3 \cdot 2$	1.9		245	< 1.8	1.7
280	$< 4 \cdot 4$	2.7	044	5.6	5.4		246	< 1.6	0.1
330	13.4	-12.9	045	$2 \cdot 2$	0.9		361	< 1.7	-l·l
350	5.8	-5.7	046	$2 \cdot 0$	-1.0		362	3.8	3.7
370	$8 \cdot 2$	8.4	051	< 1.8	- 1·0		363	< 1.8	-0.5
390	< 4.8	1.6	052	4.4	5.8		364	4.6	4.4
440	13.8	14.0	053	< 2.0	-l·9		365	< 1.6	1.1
460	< 2.8	0.9	054	10.4	10.7		481	< 1.8	-l·3
<b>480</b>	<b>4</b> ·2	<b>4</b> ·9	055	$< 2 \cdot 1$	-1.3		482	3:3	3.8
550	15.6	15.3	056	7.1	6.3	İ	483	2.4	-1.9
570	< 3.2	-0.3	061	16.1	17.4		112	6.9	2.8
660	7.8	-7.9	062	< 2.0	-2.9		114	4.7	4.4
680	< 3.6	1.0	063	3.6	$5 \cdot 2$		116	< 1.8	0:8
770	$6 \cdot 2$	-6.0	064	$< 2 \cdot 0$	-0.5		222	$24 \cdot 2$	$26 \cdot 1$
002	35.6	33.7	065	$< 2 \cdot 0$	0.2		224	<b>8</b> ∙3	'9.6
004	$5 \cdot 2$	4.1	071	3.0	3.0		226	< 1.8	1.8
006	$< 2 \cdot 1$	0.8	072	$2 \cdot 0$	$1 \cdot 2$		332	10.8	-9.8
011	<b>4</b> ·8	$2 \cdot 2$	073	6.1	7.5		334	$5 \cdot 3$	-3.9
012	12.4	11.7	074	$< 2 \cdot 1$	-0.7		336	< 1.6	0.7
013	6.6	-6.4	075	6.4	6.3		442	14.0	$13 \cdot 2$
014	11.4	11.0	081	$2 \cdot 9$	-4.2		444	5.8	5.8
015	8.9	-8.3	082	3.4	5.5		552	8:2	7.6
016	5.6	5.4	083	$< 2 \cdot 0$	- l·6		554	< 1.5	0.7
017	$2 \cdot 4$	-2.5	084	$< 2 \cdot 0$	0.7		662	3.7	-4.3
021	<b>48</b> ·6	46.2	901	2.4	1.3		664	< 1.8	-0.5
022	< 1.6	-0.5	902	<b>4</b> ·0	$4 \cdot 2$		772	4.9	- <b>4</b> · <b>4</b>
023	16.2	$15 \cdot 1$	903	3.1	0.7				

\* The origin is at  $\frac{1}{4}$ ,  $\frac{1}{4}$  with respect to the origin in the *Internationale Tabellen*. The values from which these structure factors were calculated are  $x_{\text{Cl}} = 0.275$ ,  $z_{\text{Cl}} = 0.204$ ,  $x_{\text{B}} = 0.105$  and  $z_{\text{B}} = 0.385$ . The differences between structure factors calculated from these and from our final parameters (Table 1) are well within our uncertainties in the  $F_o$ 's.

probable errors in the parameters were calculated from the residuals  $\sqrt{w}$ .  $|F_c - F_o|$  on the assumption that these differences are random errors. The final parameters



Fig. 5. Topological diagram of the  $B_4Cl_4$  molecule with bond lengths shown on the right and bond numbers on the left.

and their corresponding probable errors are summarized in Table 1. The Fourier results have been corrected for back-shift, which is -0.04 Å for  $x_{\rm B}$  and within  $\pm 0.01$  Å for all other parameters. The temperature factor constant B = 3.5 Å<sup>2</sup> was found from the leastsquares treatment, and the factor exp  $(-B\sin^2\theta/\lambda^2)$ has been multiplied into the  $F_c$  of Table 2 which shows a comparison of observed and calculated structure factors. The usual index of reliability,  $\Sigma ||F_c| - |F_o|| \div$  $\Sigma |F_o|$  is 0.09 when non-observed reflections are omitted, and 0.14 if they are included.

The molecular dimensions, calculated from the averaged parameters of Table 1, are  $B_1B_2 = B_2B_3 = B_3B_4$  $= B_4B_1 = 1.71\pm0.04$  Å,  $B_1B_3 = B_2B_4 = 1.69\pm0.04$  Å, all B-Cl =  $1.70\pm0.03$  Å, four Cl  $\cdots$  Cl =  $4.50\pm0.01$  Å, and two Cl  $\cdots$  Cl =  $4.46\pm0.01$  Å. The molecule, of symmetry  $D_{2d}$ , is shown in Fig. 5. The two types of Cl  $\cdots$  Cl distances are different within the probable errors, and while we feel that the deviation from  $T_d$ symmetry is real this deviation is so slight that it may be associated with the molecular packing in the solid, and the true symmetry of isolated molecules in the gas phase may well be  $T_d$ .

Bond orders in B<sub>4</sub>Cl<sub>4</sub> have been discussed in a preliminary note (Atoji & Lipscomb, 1953) in which only the final Fourier parameters were reported. Bond orders for the final averaged parameters are 1.00 for BCl, 0.66 for the longer B-B bonds, and 0.71 for the shorter B-B bonds, thus yielding a total bond order of 8.04 for the molecule. These values, based on normal B-Cl and B-B single bond distances\* of 1.70 and 1.60 Å, respectively, are insignificantly different from those previously reported by us. While the mean B-B-B valency angle is  $60^{\circ}$ , as it is in the tetrahedral  $P_{4}$  and  $As_{4}$  molecules, the hybridization must be quite different, inasmuch as d orbitals are not available for boron. That the  $60^{\circ}$  angle represents some sort of strained bond seems probable, and seems to be supported by the average B-B-Cl angle of  $144.6^{\circ}$ , which seems larger than normal, even for boron.

\* These distances are obtained from the covalent radius of 0.80 Å for B (Hedberg, 1952) and 0.99 Å for Cl, plus a shortening of 0.09 Å for B-Cl due to the electronegativity difference between B and Cl (Schomaker & Stevenson, 1941). The molecular packing is quite reasonable as is indicated by the intermolecular  $\text{Cl} \cdot \cdot \cdot \text{Cl}$  distances of 3.63, 3.74 and 3.87 Å. These values are consistent with the van der Waals radius of 1.8 Å usually assigned to Cl.

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# Traitement Statistique des Erreurs dans le Cas d'une Structure Pseudo-Centrosymétrique

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#### (Recu le 13 novembre 1952)

A statistical calculation has been used to determine a relation between the empirical function  $\langle (F_o^2 - F_c^2)^2 \rangle / \langle F_c^4 \rangle$  and the mean error in atomic positions in the following cases: (a)  $F_o$  and  $F_c$  non-centrosymmetrical; (b)  $F_o$  and  $F_c$  centrosymmetrical; (c)  $F_c$  centrosymmetrical,  $F_o$  noncentrosymmetrical; (d) the analogue of (c) but in which the atoms are approximately situated on a symmetry element.

On peut être amené, dans la détermination des structures cristallines, à admettre que les atomes adoptent, en première approximation, une configuration centrosymétrique, alors qu'en réalité la structure n'a pas de centre de symétrie. Les séries de Fourier calculées avec les phases correspondant à cette hypothèse sont centrosymétriques: si l'écart entre la structure centrosymétrique et la structure réelle est faible, il peut être difficile de déterminer les positions correctes des atomes, ou même d'estimer l'erreur commise. C'est le cas qui s'est présenté au cours de l'étude de la structure cristalline de NaOH.4H<sub>2</sub>O (Hemily, 1952). Cette substance cristallise dans le système monoclinique, groupe de symétrie C2; on a résolu sa structure en supposant que tous les atomes étaients contenus dans le plan y = 0, qui devient ainsi un plan miroir (le groupe de symétrie devient C2/m). Une fois la structure déterminée, dans l'hypothèse centrosymétrique, nous avons cherché à connaître l'écart moyen des atomes des positions centrosymétriques.

Nous nous proposons ici de déterminer les lois de distribution des parties réelle et imaginaire de la différence  $\Delta F$  entre les facteurs de structure corre-

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